

January '16

February						
M	T	W	T	F	S	S
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29						

Wk 01

# Boolean Algebra

## Logic gates

01  
Friday

Boolean algebra is a system of mathematical logic and is different from both ordinary algebra and the binary number system. In Boolean algebra  $1+1=1$ , in it the variables permitted to have only two values true or false (1 & 0) and the algebraic operations on the variables are limited to those defined as AND, OR, NOT.

Boolean two variables true and false may be represented by on or off states of electronic switching circuits. On account of such functioning of switching circuits, Boolean algebra becomes of practical significance and is implemented through these switching that act as electronic logic circuits.

### Logic gates →

A logic gate is an electronic circuit which makes logic decisions, it has one output and one or more inputs. Logic gates are the basic building blocks from which most of the digital systems are built up. They implement the hardware logic function based on the logical algebra called Boolean algebra.



Saturday

002-364

The OR Gates

	M	T	W	T	F	S	S
					1	2	3
	4	5	6	7	8	9	10
	11	12	13	14	15	16	17
	18	19	20	21	22	23	24
	25	26	27	28	29	30	31

This operation is represented by the symbol + and the operation is written as

$$A \text{ OR } B = A + B = C$$

which means that if A is true OR B is true then C will be true.

Truth table for OR operation

$$A + B = C$$

$$0 + 0 = 0$$

$$0 + 1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 1$$

	0	1	2	3
A	0	0	1	1
B	0	1	0	1
C	0	1	1	1

Truth table

OR function

The electronic symbol for a two input OR gate is shown in fig a and its equivalent switching circuit

03 Sunday fig b.

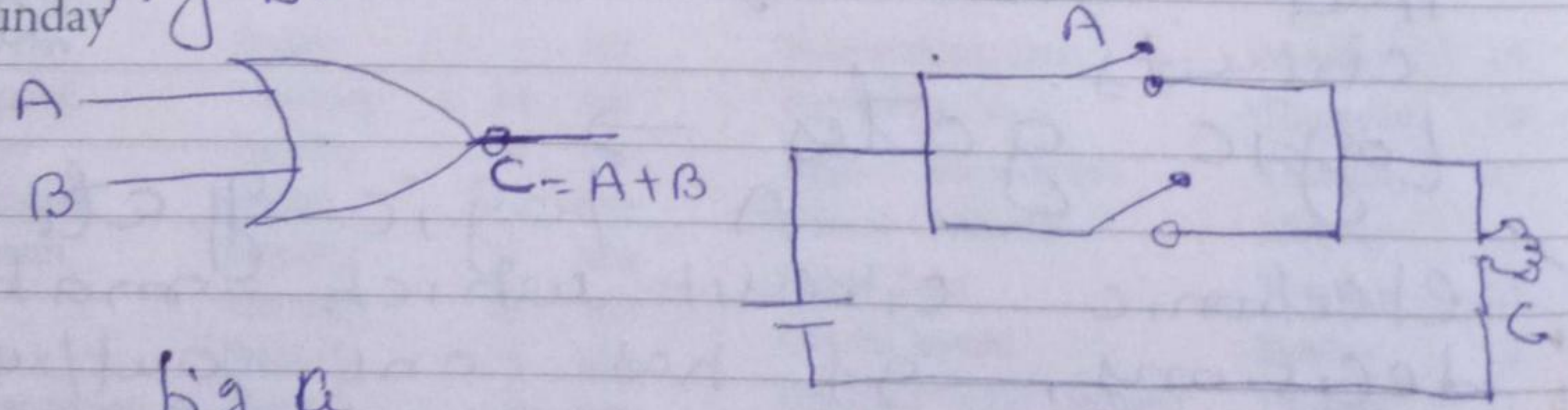


fig a

fig b

The two inputs have been marked A and B and the output as C. In (b) if all inputs are at zero level, diodes do not conduct. Current through



February

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Wk 02  $R_L$  is zero and ~~output level~~ Monday taken across  $R_L$  is zero.

② THE AND OPERATION →

this operation is represented by the symbol  $\cdot$  and the operation can be written as

$$A \text{ AND } B = A \cdot B = AB = C$$

which means that if A is true AND B is true and C will be true.

Truth table for AND operation

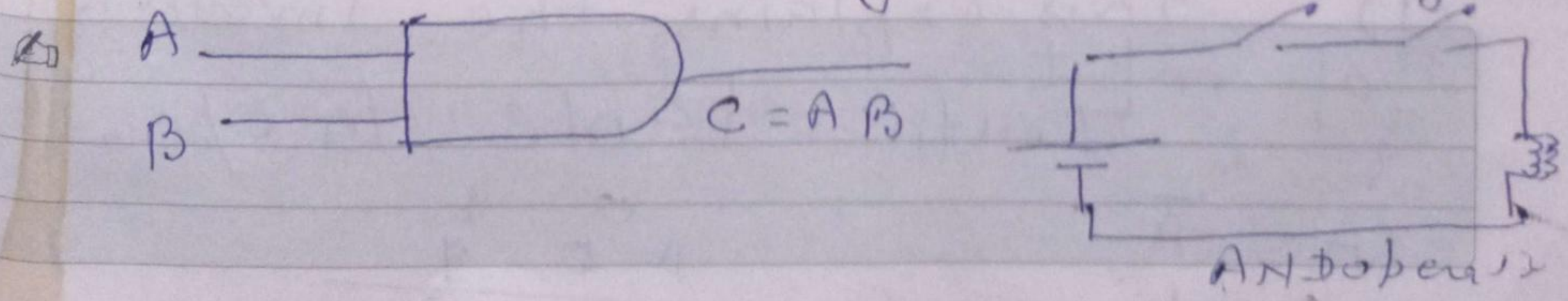
$A \cdot B = 0$	0	1	2	3
0 0 = 0	A	0	1	1
0 1 = 0	B	0	1	1
1 0 = 0	C	0	0	0
1 1 = 1				1

AND function

truth table

AND Gate →

The electronic or logic symbol for a 2 input AND gate is shown in fig 2a and its equivalent switching circuit in fig b.





Tuesday

005-361

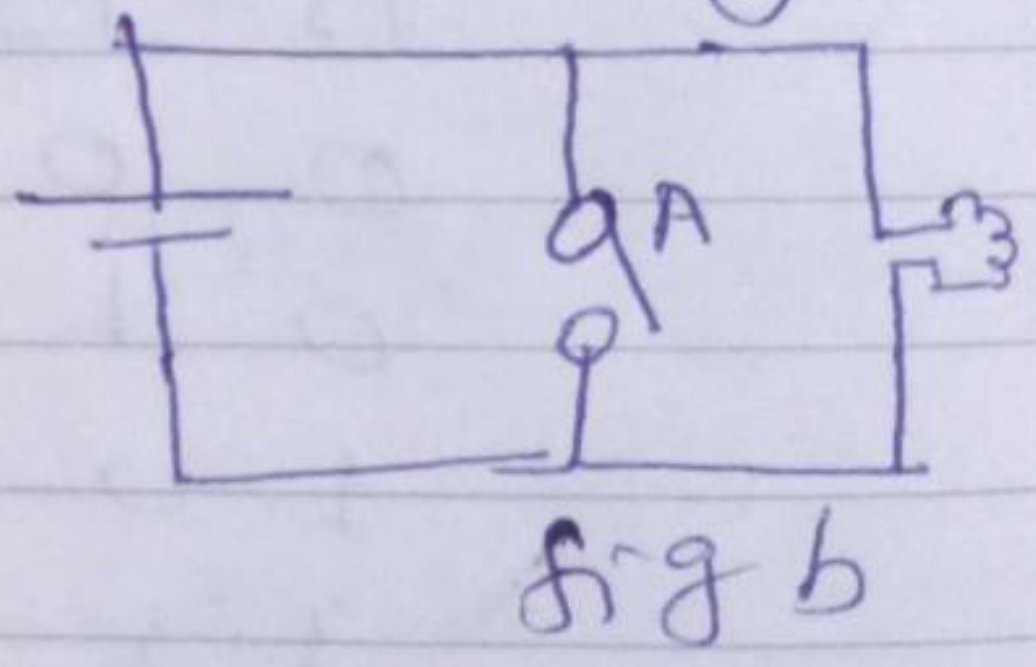
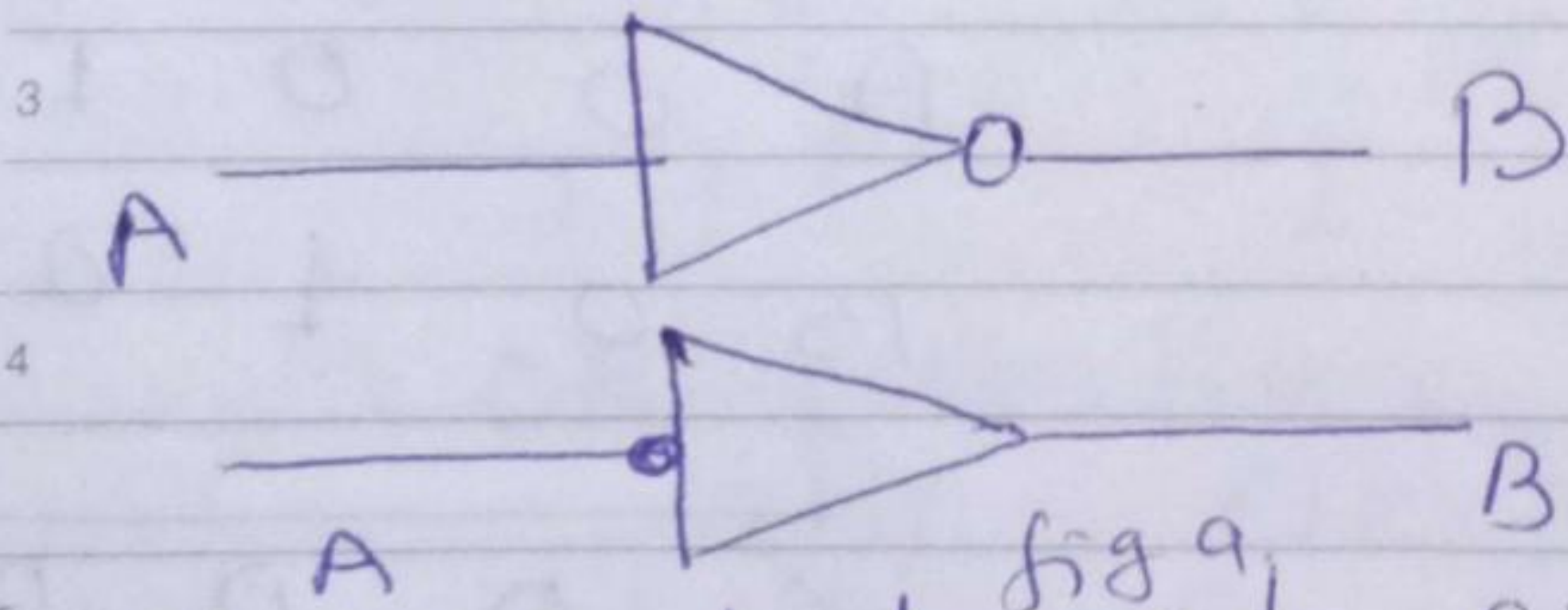
M	T	W	T	F	S	S
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The AND gate gives an output only when all its inputs are present.

3 The NOT Gate  $\rightarrow$  It is so called because its output is

NOT the same as its input. It is also called an inverter because it inverts the input signal. It has one input and one output shown in

fig 3a. This operator is represented by a bar e.g.  $\bar{A}$ . The operation is also called as complementation or negation (inversion). The NOT gate is thus called complementary circuit.



The symbol of circle actually represents the inversion and the triangle an amplifier.

In fig b when switch A is closed (input 1) the bulb does not glow (0) because closed switch present a short circuit across the bulb. Similarly when switch is open (0) bulb glows (1). This explains the inversion of input.

Truth table for operation

$A = \bar{A}$   
 $0 = 1$   
 $1 = 0$

	0	1
A	0	1
B	1	0



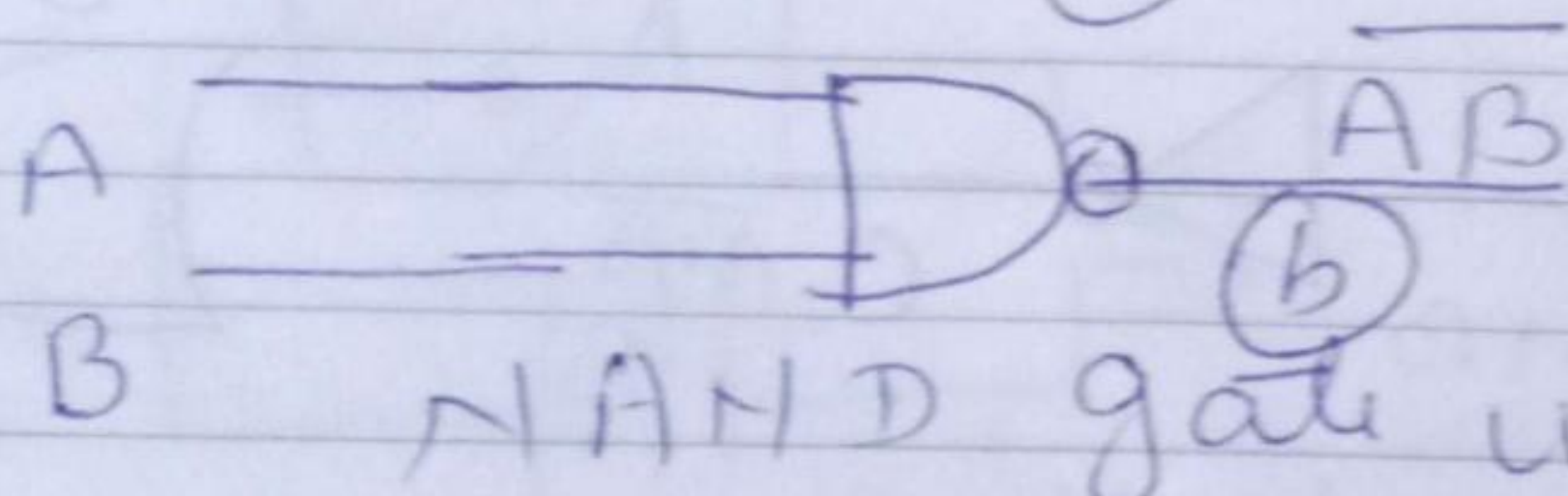
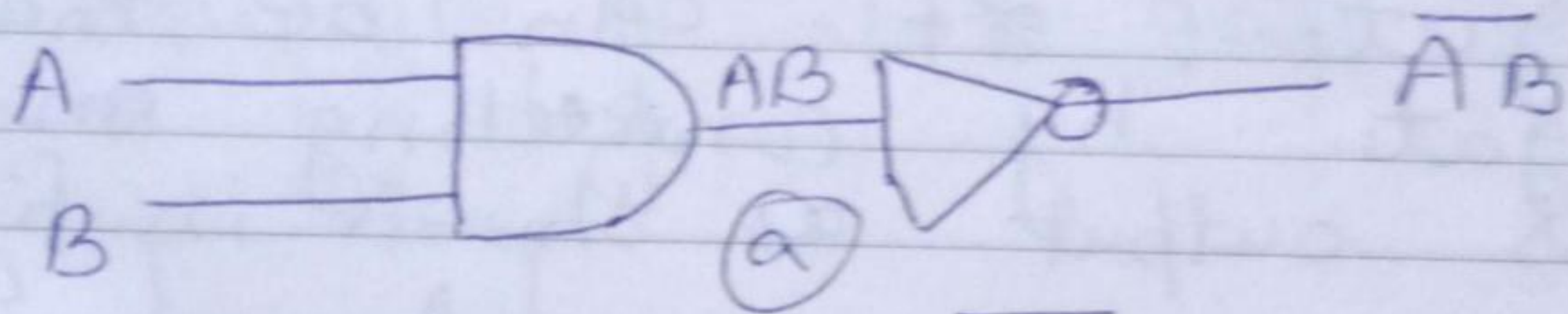
February

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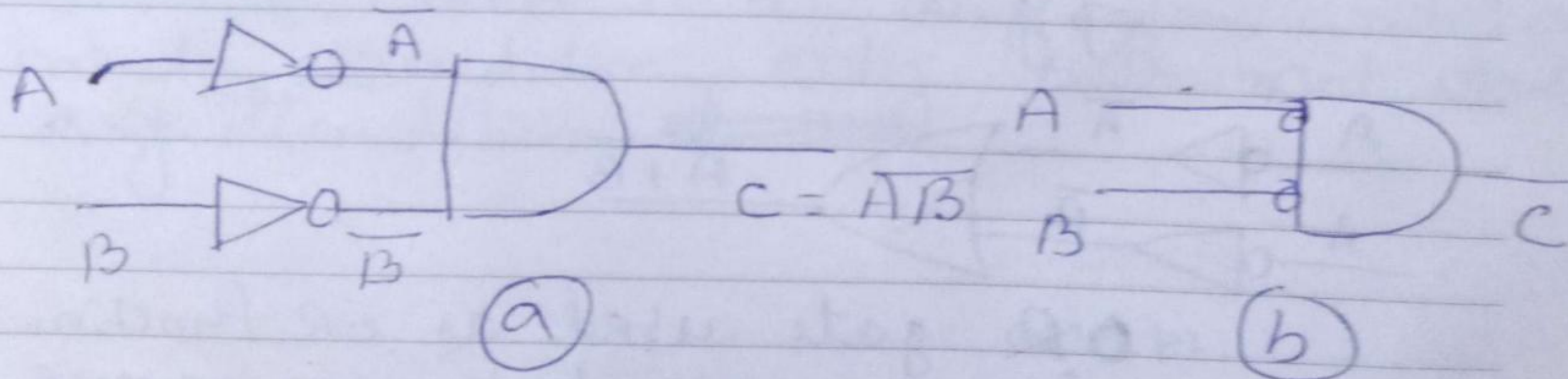
Bubbled gates → Wednesday

A bubbled gate is one whose inputs are NOTed or inverted i.e. it is negated gate. NAND & NOR gate can perform both the AND function or OR function. Thus these two gates are called Universal building blocks.

NAND gate → NAND gate symbolically in which a NOT gate follows an AND gate (inverter). The inputs A & B are ANDed, yielding  $AB$  and then inverted,  $\overline{AB}$



NAND gate used AND function



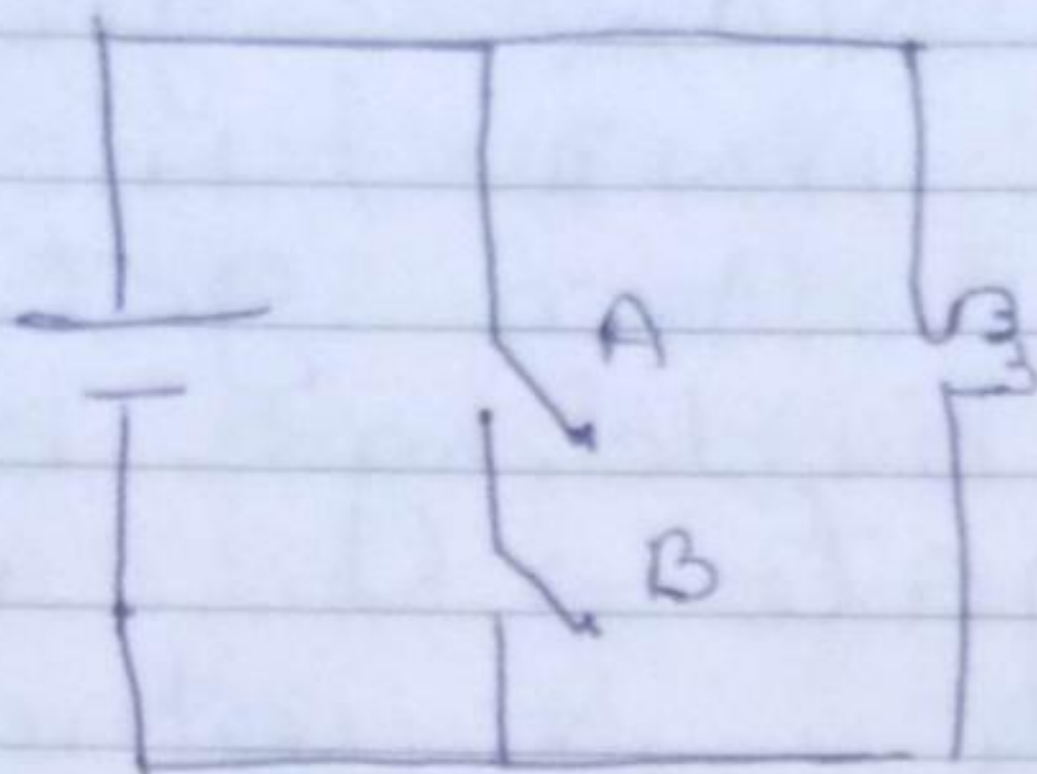
The Truth table →

	AND	NAND		
$C = AB$	$=$	$\overline{AB}$		
	A	B	0	1
	0	0	1	1
	0	1	0	1
	1	0	1	0
	1	1	1	0



Thursday

Fig 6 shows the electrical analog of this gate obviously the lamp will not glow if both inputs A and B are in logic "1" state i.e. switches are closed.



electrical analog of NAND

The NOR gate  $\rightarrow$  It is NOT-OR gate. It can be made of an OR gate by connecting an inverter in its output as shown in fig.

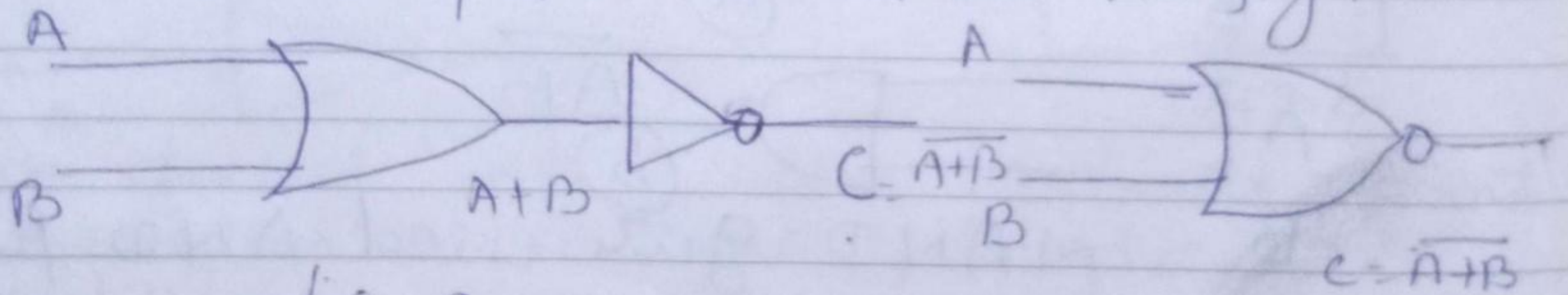
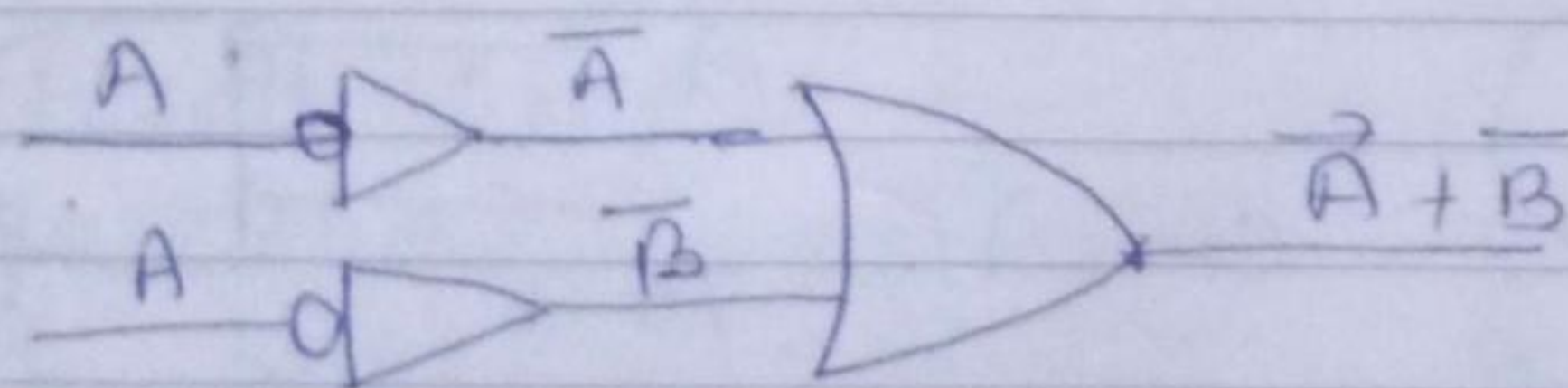


fig a



NOR gate used as OR function

A NOR function is just the reverse of the OR function.

The output equation is just given by

$$C = \overline{\bar{A} + \bar{B}}$$



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Wk 02 Logic operation <sup>008-258</sup>

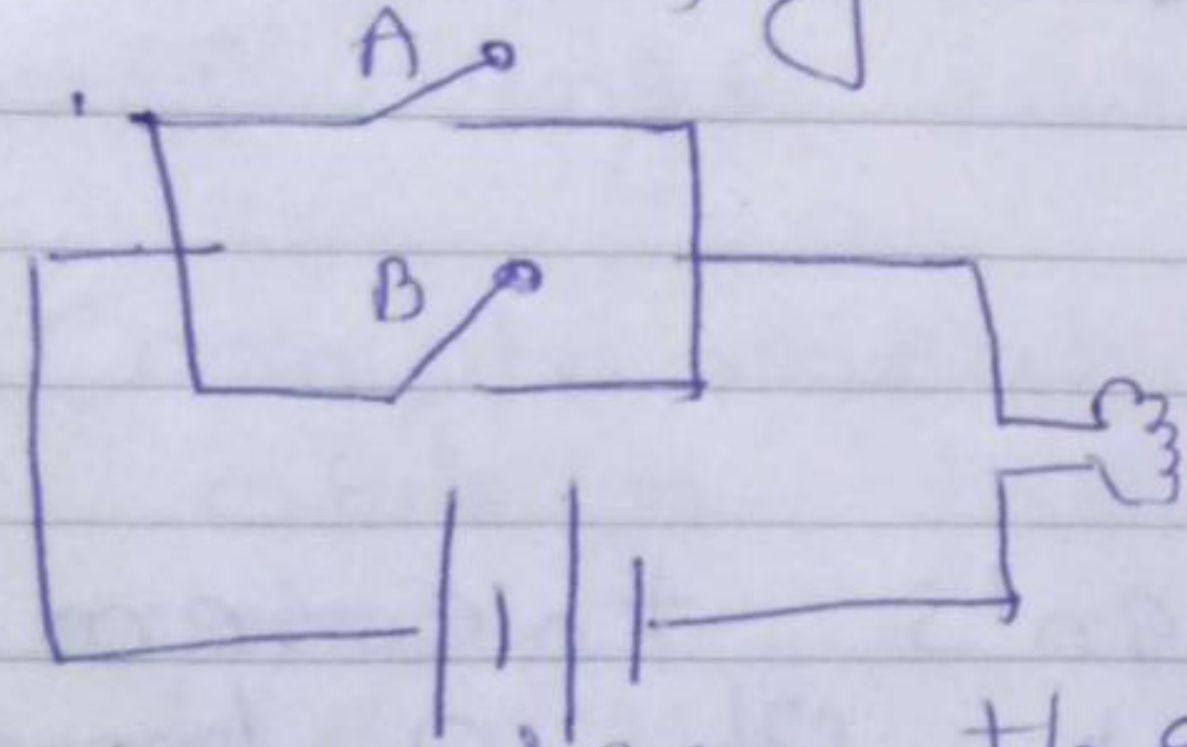
A NOR gate will have an output of 1 only when all its inputs are 0. Obviously, if any output is 1, the output will be 0. In a NOR gate, the output is true only when all inputs are false.

Truth table

$$C = \overline{A+B}$$

A	B	C = $\overline{A+B}$
0	1	0
1	0	0
1	1	0
0	0	1

The equivalent NOR gate function is shown in fig



It is seen that lamp glows under 00 input condition only but not under any <sup>input</sup> condition.